AB: Q201 EXAMINATION REVIEW PRACTICE

TECHNOLOGY SECTION: Round answers to three decimal places.

1. The velocity of a particle moving along a horizontal is given as $v(t) = 8\cos(t) + \ln(\sin(t) + t^2)$ on $0.1 < t \le 8$.

A. On what time interval is the particle moving to the right? Justify.

- B. What are the velocity and acceleration at time t = 5? Round answers to three decimal places.
- C. Is the particle speeding up or slowing down at t = 3.5? Justify.

- 2. The derivative of f is given by $f'(x) = e^{x^2} 5x^3 + x$ on $0 \le t < 3$
- A. On what interval is *f* decreasing? Justify.
- B. At what *x*-value(s) does *f* have a relative maximum? Justify.
- C. On what interval is *f* concave upward? Justify.

NO TECHNOLOGY SECTION

1. Let *f* be defined by $f(x) = \ln(2 + \sin x)$ for $\pi \le x \le 2\pi$.

Find the absolute maximum value and the absolute minimum value of f using the closed interval test.

2. A. When is the graph of f(x) concave upward if $f''(x) = (x-1)(x+2)^2 e^{x^2}$. Justify. B. How many points of inflection are on f? Justify. 3. A particle moves along a horizontal line. It's position at time t is given as

$$s(t) = \frac{2}{3}t^3 - \frac{5}{2}t^2 - 3t \; .$$

On what time interval is the particle slowing down? Justify.

The graph of f'(x)

4. Consider the graph of the <u>derivative</u> of f below.

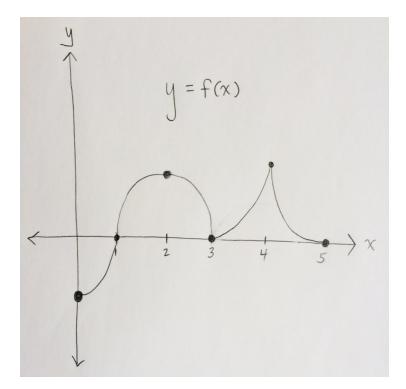
A. For what x – values does f have a local minimum? Justify.

B. On what interval is *f* increasing? Justify.

- C. On what interval is *f* concave upward? Justify.
- D. How many points of inflection are on f?

GRAPH THEORY

5. Below is Steven's graph of y = f(x).



THE CHART REPRESENTS STEVEN'S GRAPH

| x | 0 | 0 < x < 1 | 1 | 1 < x < 2 | 2 | 2 < <i>x</i> < 3 | 3 | 3 < <i>x</i> < 4 | 4 | 4 < <i>x</i> < 5 | 5 |
|-----------------------|---|-----------|-----|-----------|---|------------------|---|------------------|---|------------------|---|
| f(x) | | | | | | | | | + | | |
| f'(x) | | | DNE | | | | | | | | |
| $f^{\prime\prime}(x)$ | | | | | | | | | | | |

FILL IN EACH BLANK IN THE CHART ABOVE WITH ONE OF THE FOLLOWING:

- + for positive
- for negative
- **0** for zero

DNE for Does not Exist